

## I- Motivation and overview of 1D models of plume rise

### 1 - 0D/1D models of plume rise are useful tool to understand, predict and reconstruct volcanic sulfur injections into the atmosphere.

- Three examples of application (Fig. 1):
- Near real-time mass eruption rate (MER) from plume height measurement during eruptive crisis
  - Plume height from MER, e.g. when designing scenarios for future eruptions
  - Plume height from deposit when reconstructing the forcing of ancient eruptions

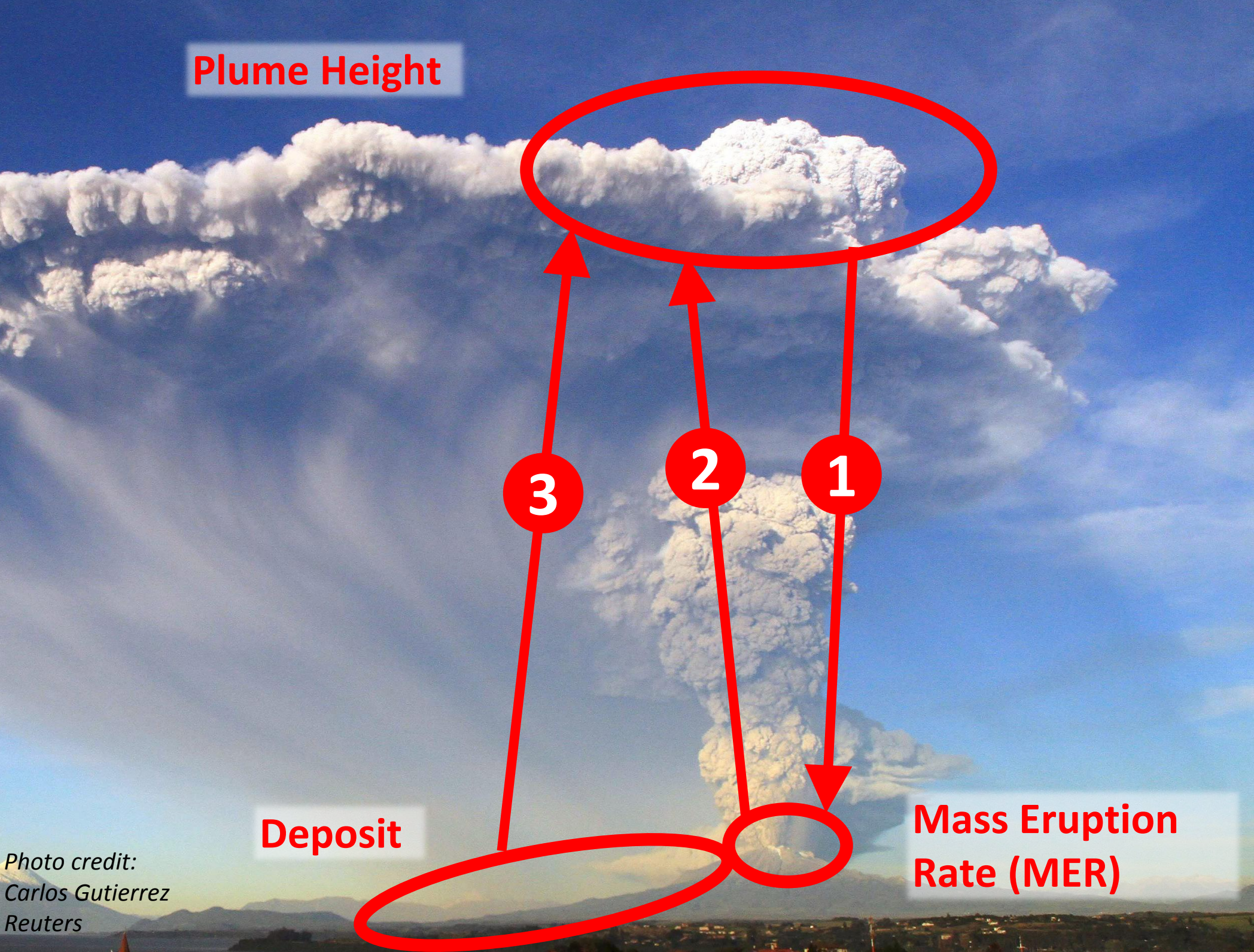


Fig. 1: 2015 eruption of Calbuco (Chile)

### 2- Effective model predictions are hindered by uncertainties related to parameter calibration.

Can you answer the following questions, for the Calbuco 2015 eruption, using the 1D models runs on Fig. 2:

- Given measured plume height, what is the order of magnitude of the MER?
- Given measured MER, is there a significant stratospheric injection of SO<sub>2</sub>?

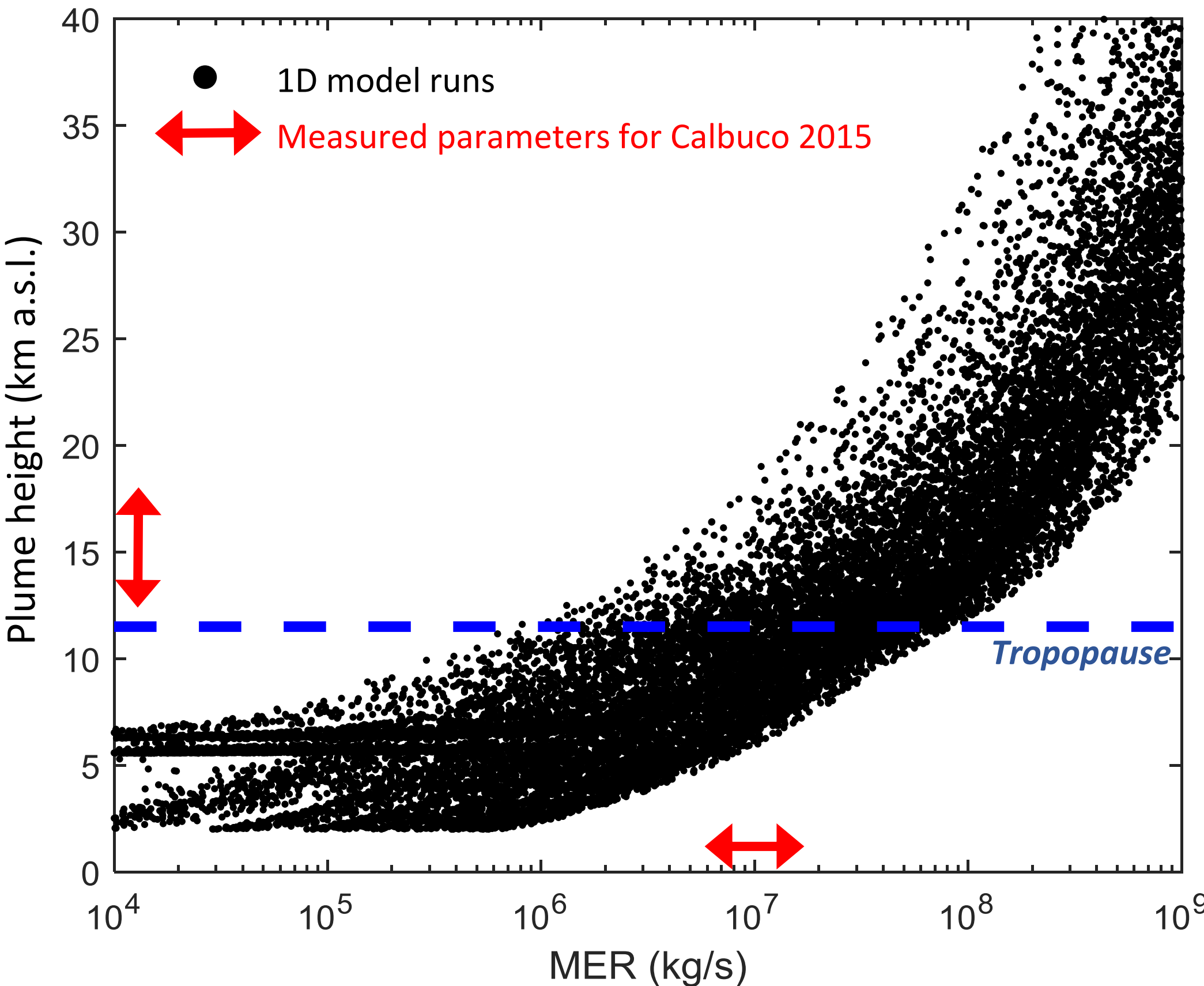


Fig. 2 (modified from ref. 1): 1D model runs with atmospheric conditions of the Calbuco 2015 eruption. The spread is due to model parameter uncertainties.

### 3 - The wind entrainment coefficient $\beta$ and condensation rate $\lambda$ are the major sources of uncertainty in 1D plume models.

- Main assumptions of 1D models<sup>1</sup>:
- Mass/momentum/heat fluxes conserved along the plume centerline
  - Steady source/atmospheric conditions
  - Top-hat radial distribution of plume properties
  - Entrainment: Influx of atmosphere at plume edge with velocity  $u_e$  (Fig. 3)
  - Condensation: Entrained atmospheric water vapor condensed at rate  $\lambda$

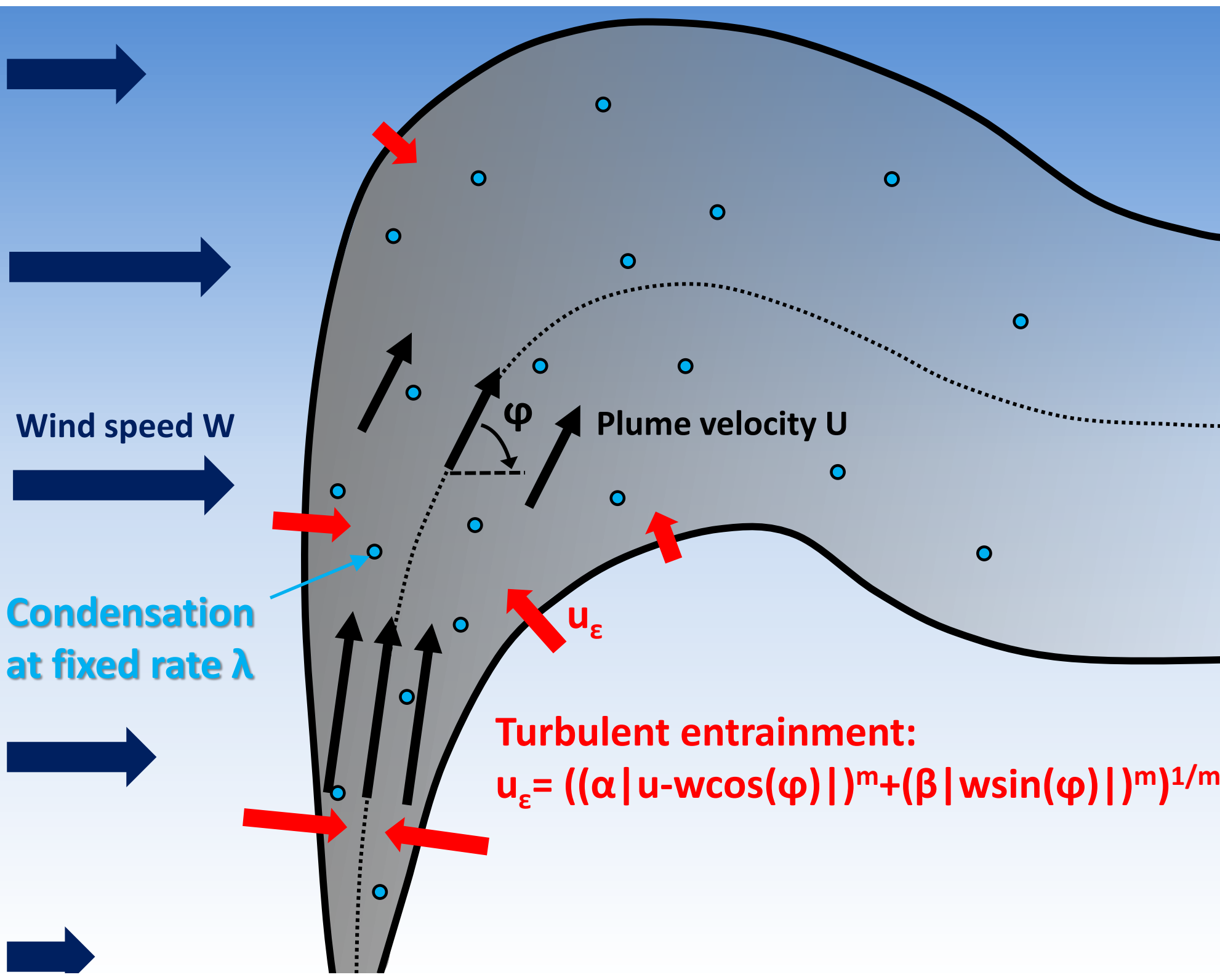


Fig. 3 (modified from ref. 1): Key concepts for 0D/1D plume models

## II- New datasets to evaluate models for volcanic plume rise

### 1 – We compile an unprecedented database of plume heights and MERs constrained independently<sup>2</sup>:

- Largest database before our study<sup>3</sup>: 25 eruptive phases and no uncertainties
- New database: 94 eruptive phases and uncertainties on height and MER; atmospheric conditions from NCEP/NCAR reanalysis

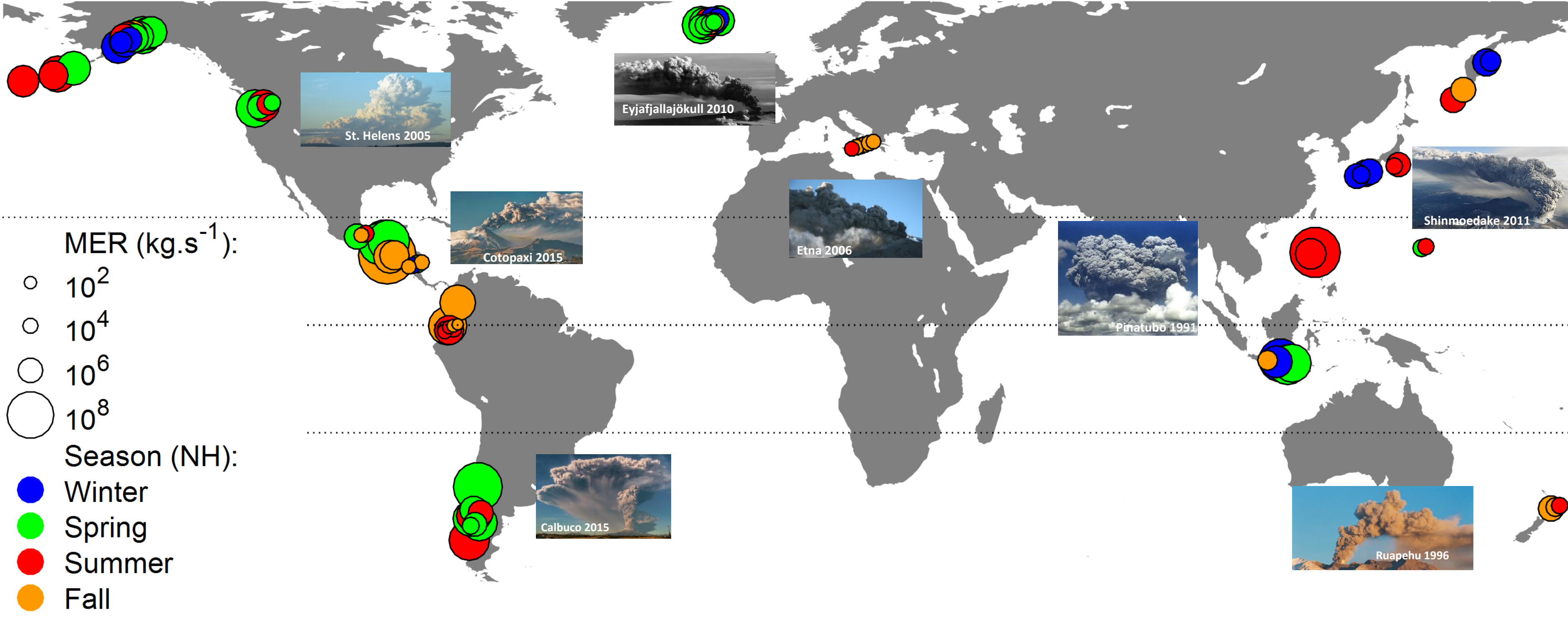


Fig. 4 (modified from ref. 1): Location, MER and season of the 94 eruptive phases of the new database. Pictures show a few select examples.

→ We use the eruptive parameter database and lab experiments to constrain and evaluate 0D and 1D plume models, along with Monte Carlo simulations to account for uncertainties in both datasets<sup>1,2,5</sup>

### 2 - New lab experiments covering the same dynamical regimes as explosive eruptions, overcoming a major limitation of previous studies<sup>2,4</sup>

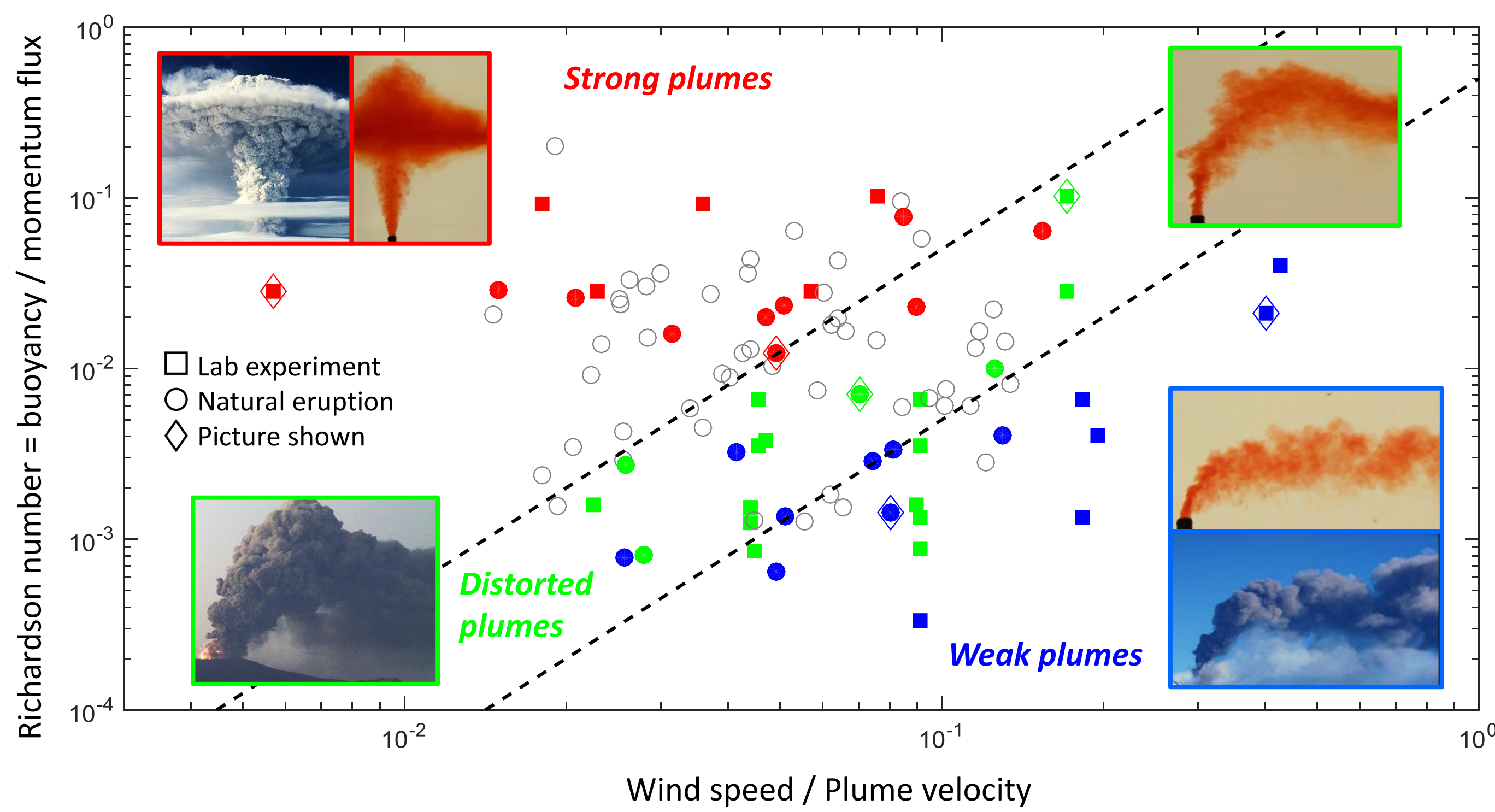


Fig. 5 (modified from ref. 2): Richardson number and velocity ratio for the new database of eruption source parameters and analog laboratory experiments. Colors highlight different plume shape regimes.

## III- New insights on 1D and 0D models parameterizations and performance

### 1 – The wind entrainment coefficient $\beta$ is small

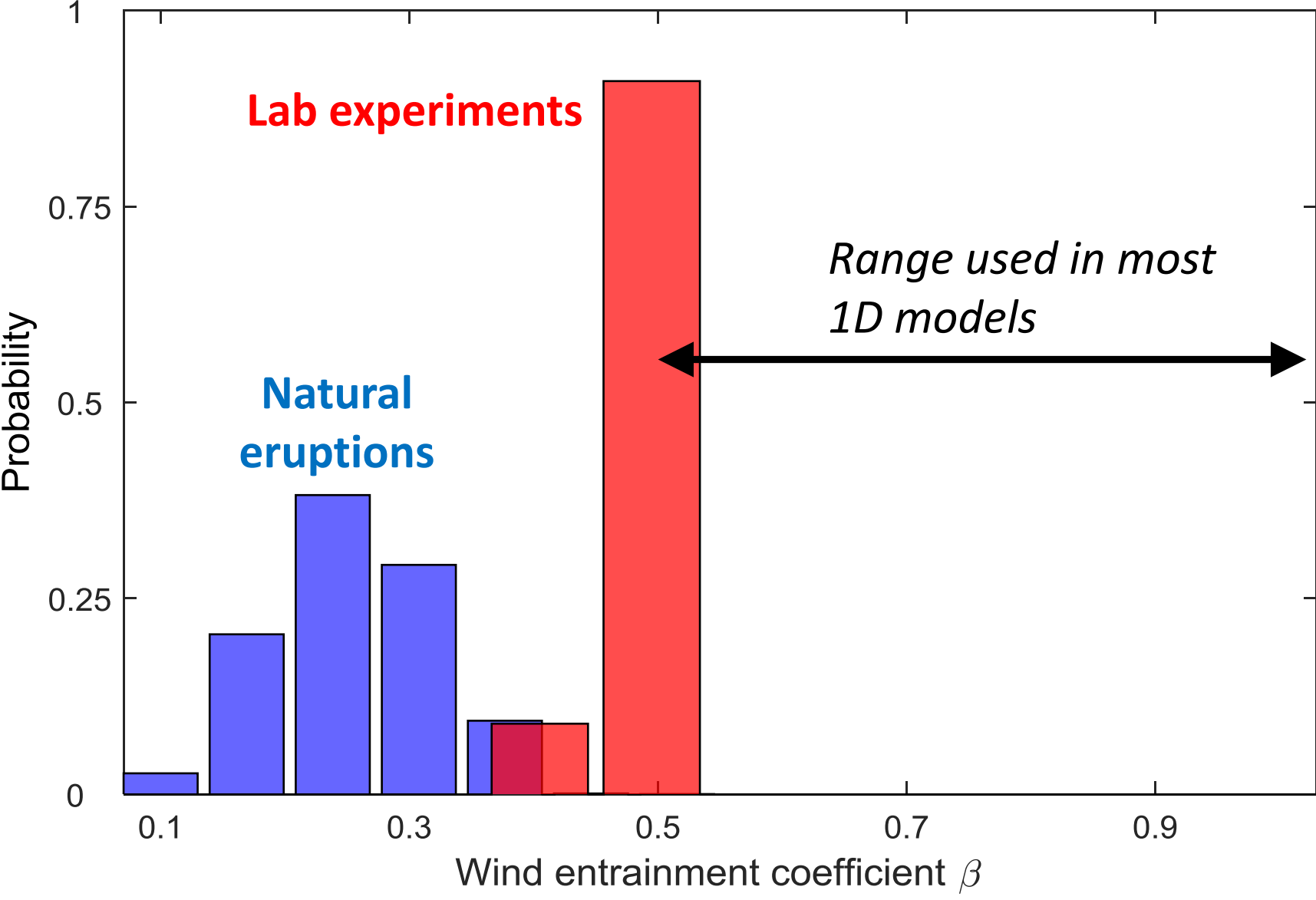


Fig. 6 (modified from ref. 1): Probability distribution of  $\beta$  obtained by minimizing error on plume height (natural eruptions) or trajectories (lab experiment) using a Monte Carlo strategy to account for observational uncertainties

### 2- Absent condensation OR negligible impact on plume buoyancy flux

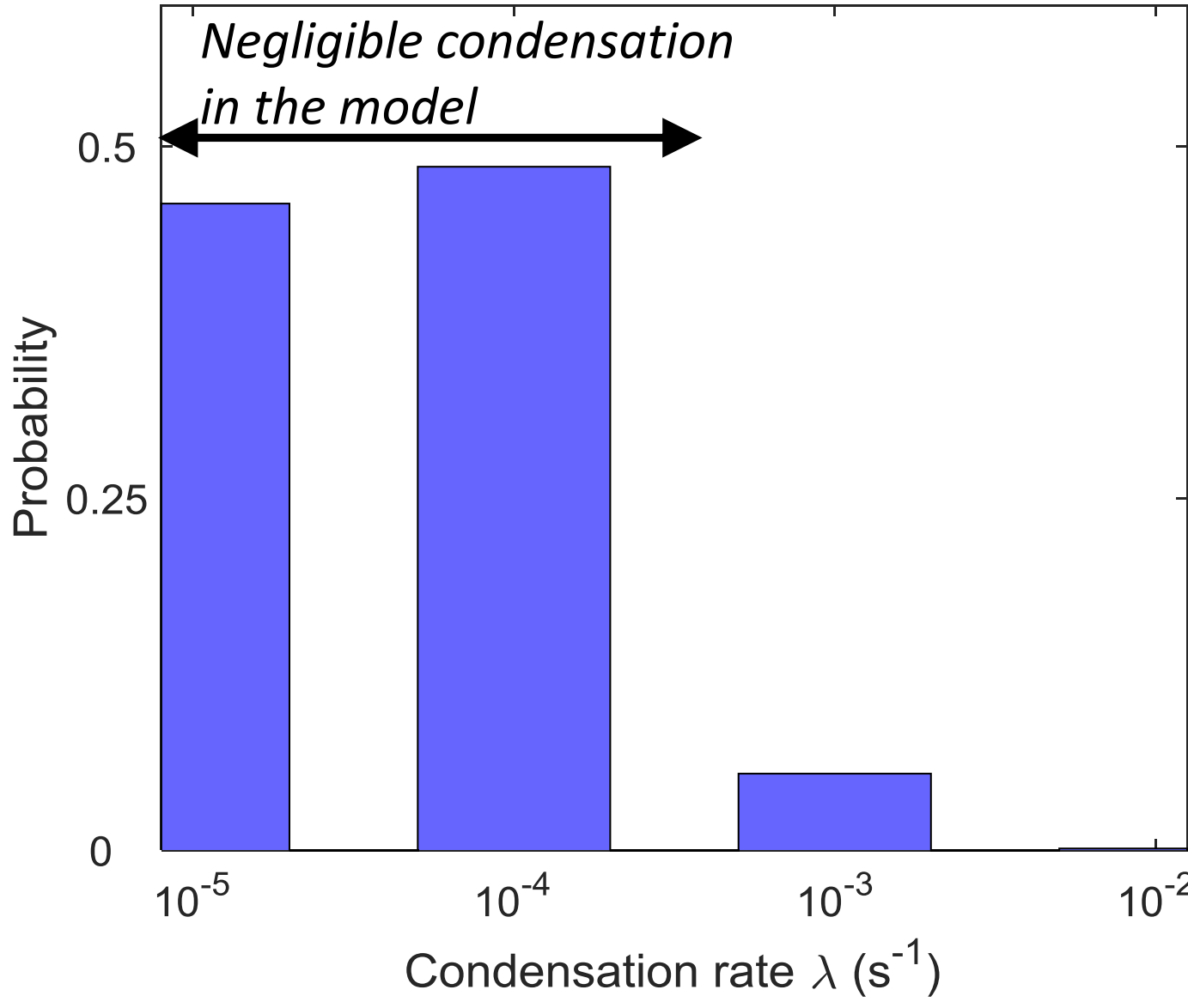


Fig. 7 (modified from ref. 1): Same as Fig. 6, but for  $\lambda$  and using only the database of explosive eruptions (no condensation in lab experiment)

### 3 – Refined calibration<sup>2</sup> of the most popular “model” for plume rise: $PH = a \times MER^b$

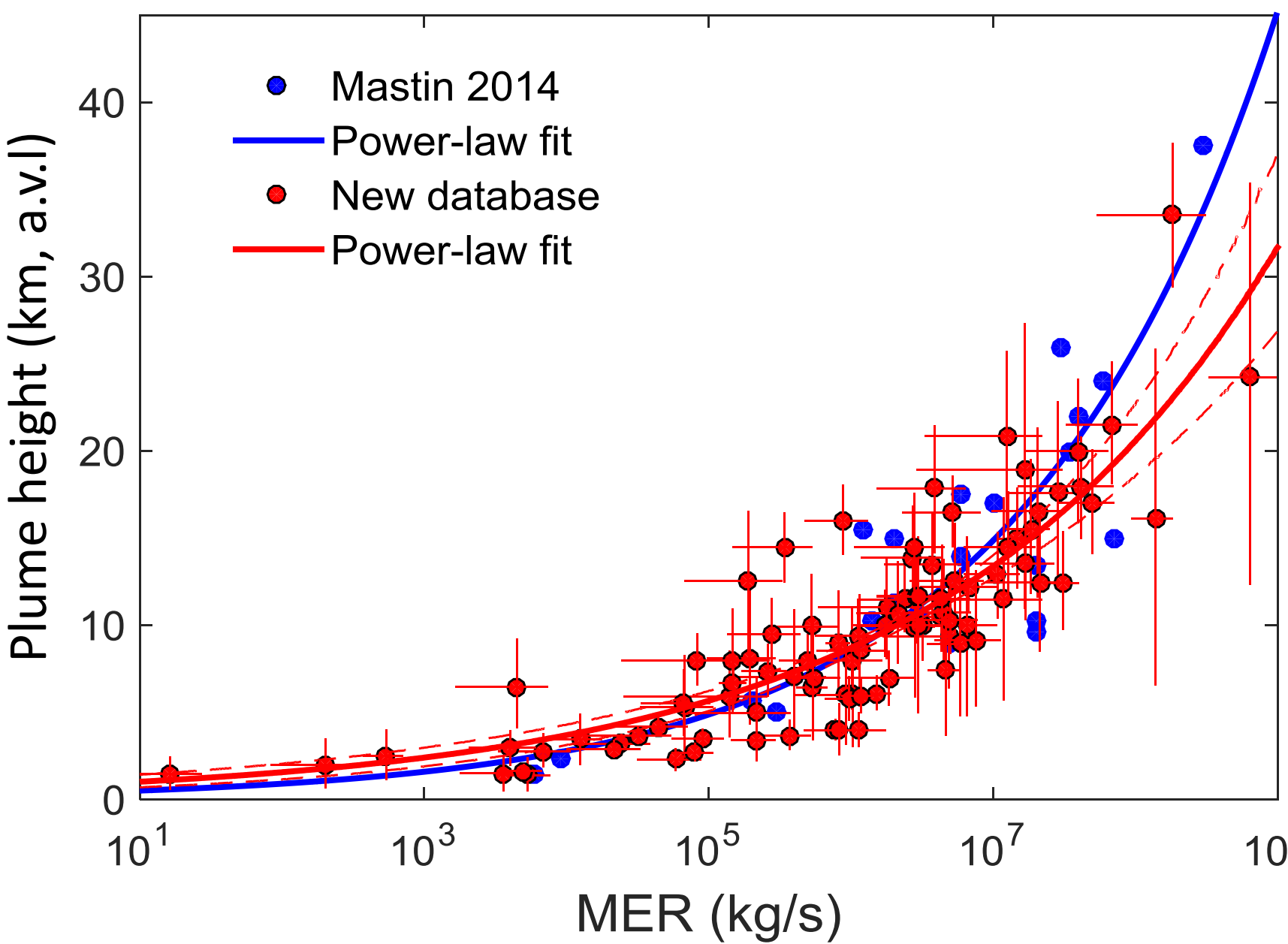


Fig. 8: Plume height vs. MER and best power-law fit for Mastin 2014 (ref. 3) and the new database of eruption source

### 4 – 1D models make significantly better plume height predictions than 0D models

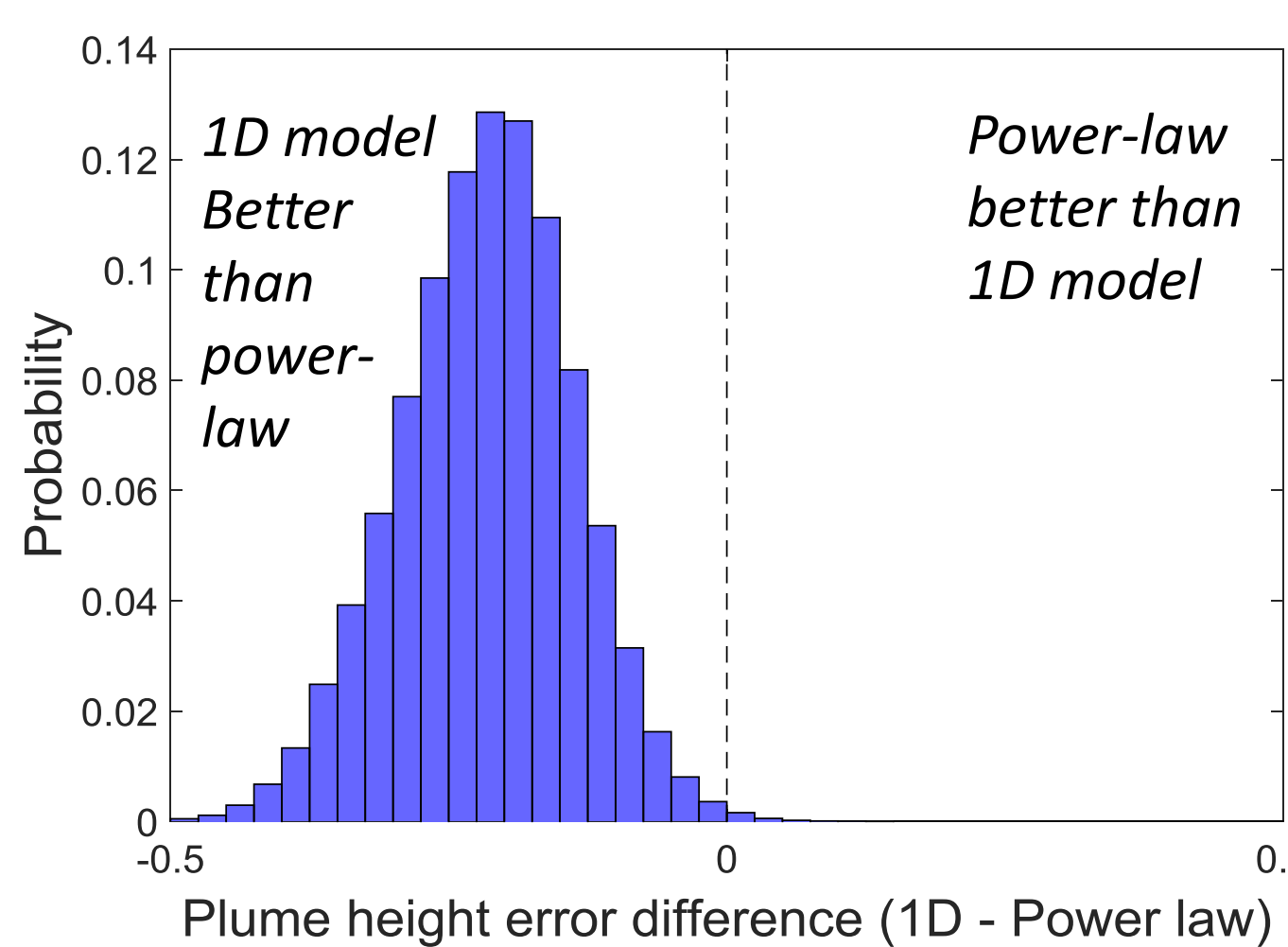


Fig. 9: Difference between error on plume height for a 1D model and a power law scaling. The error is a root mean squared error on predictions for natural eruption plume height normalized by observational uncertainties.

## IV- What MER is required to inject sulfur directly into the stratosphere?

### 1 – New datasets enable to better constrain the critical MER for stratospheric injections

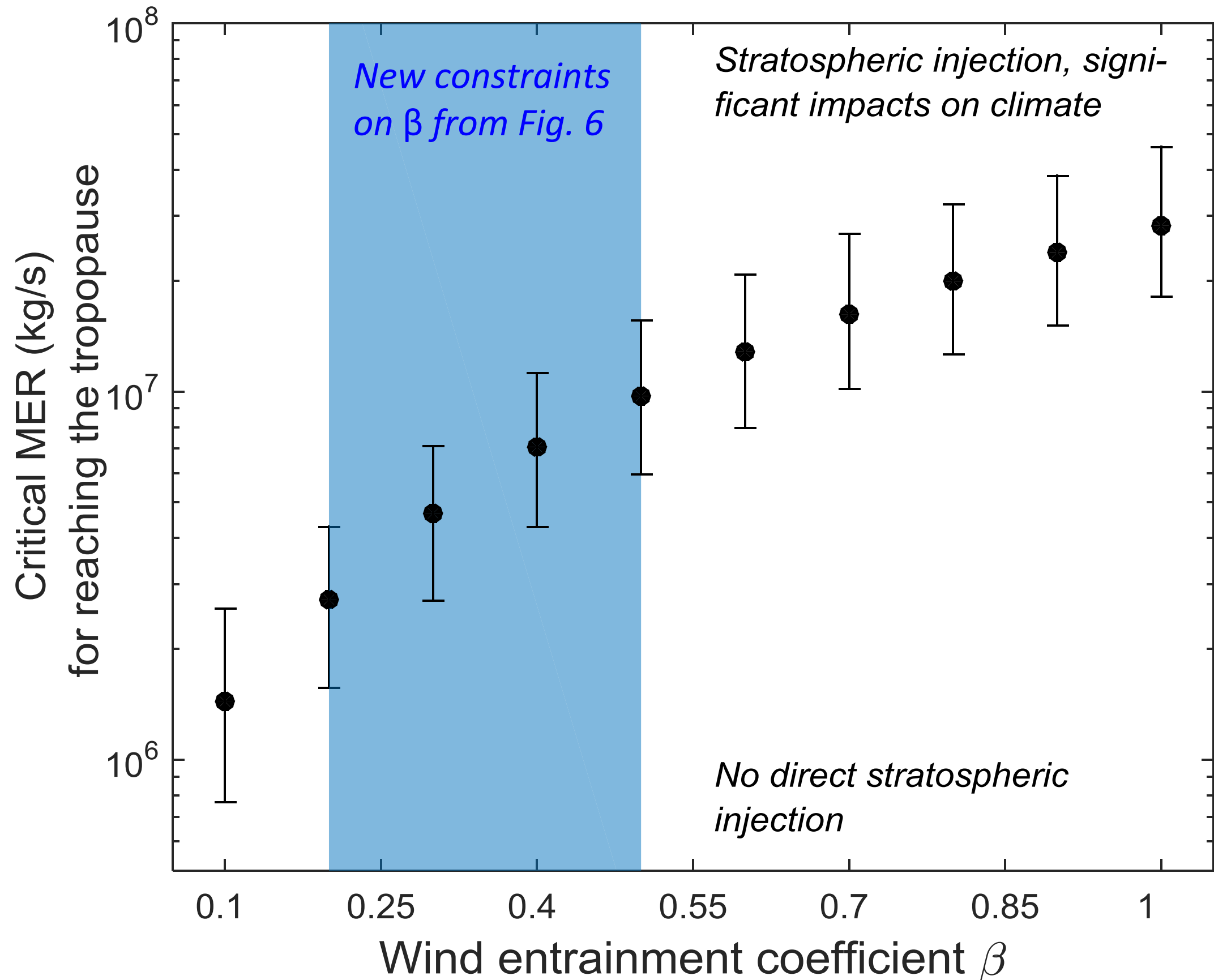


Fig. 10 (modified from ref. 5): Critical MER for stratospheric injection (right) vs  $\beta$  for the same atmospheric conditions as the 2011 Cordon Caulle eruption, and for a vent height of 1500m.

### 2 – Sensitivity of the critical MER to background climate: A new climate-volcano feedback?

- New constraints on condensation rate (Fig. 7) → relatively large MER are required to reach the tropopause
- Global warming → larger critical MER → less stratospheric SO<sub>2</sub> injections → less cooling<sup>6</sup>? More Friday at 11.30am

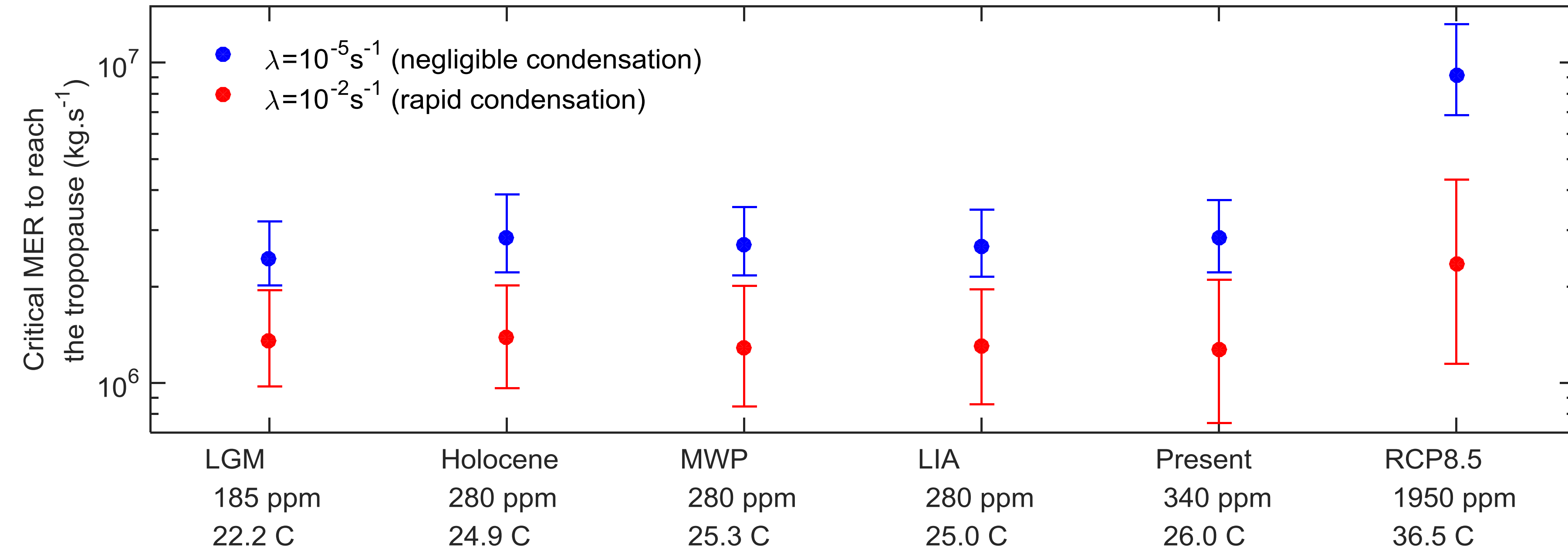


Fig. 11 (modified from ref. 1): MER required to reach the tropopause with/without condensation. Atmospheric conditions for Ecuador, from the MPI-ESM climate model and for various climates with CO<sub>2</sub> and surface temperature labeled. Vent height of 2000m. LGM= Last Glacial Maximum, MWP= Medieval Warm Period, LIA= Little Ice Age

### References

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